





**Error Propagation**

Physicists and engineers tend to make liberal use of the approximation of  $\Delta y$  by  $dy$ . One way this occurs in practice is in the estimation of errors propagated by physical measuring devices. For example, if you let  $x$  represent the measured value of a variable and let  $x + \Delta x$  represent the exact value, then  $\Delta x$  is the *error in measurement*. Finally, if the measured value  $x$  is used to compute another value  $f(x)$ , the difference between  $f(x + \Delta x)$  and  $f(x)$  is the **propagated error**.

$$\overbrace{f(x + \Delta x)}^{\text{Measurement error}} - \underbrace{f(x)}_{\text{Measured value}} = \overbrace{\Delta y}^{\text{Propagated error}}$$

*(Note: In the original image, 'Exact value' is written below 'Exact value' and 'Measured value' is written below 'Measured value'.)*

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32. **Volume and Surface Area** The measurement of the edge of a cube is found to be 12 inches, with a possible error of 0.03 inch. Use differentials to approximate the maximum possible propagated error in computing
- (a) the volume of the cube.
  - (b) the surface area of the cube.

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In Exercises 45–48, use differentials to approximate the value of the expression. Compare your answer with that of a calculator.

45.  $\sqrt{99.4}$

46.  $\sqrt[3]{26}$

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